

$$(1) \quad 1 + \frac{1}{3^2} + \frac{1}{5^2} + \frac{1}{7^2} + \dots = \frac{\pi^2}{8}$$

$$(2) \quad \frac{1}{2} + \frac{1}{1 \times 3} - \frac{1}{3 \times 5} + \frac{1}{5 \times 7} - \frac{1}{7 \times 9} + \dots = \frac{\pi}{4}$$

$$(3) \quad 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \dots = \frac{\pi}{4}$$

(1)

```
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
void main()
{
float i,y,pi,sum=0.0;
    for(i=1.0;i<=10000.0;i++){
        y=1.0/(float)pow(2.0*i-1.0,2.0);
        sum+=y;
    }
    pi=sqrt(sum*8.0);           //same as pi=pow(sum*8.0,1.0/2.0);
    printf("pi=%.6f \n",pi);   //shown as %.6f ,but test in %.20f
}

```

(2)

```
#include <stdio.h>
#include <math.h>
#include <stdlib.h>
void main()
{
float i,x,y,z,pi,sum=0.5;
    for(i=1.0;i<=100.0;i++){
        x=pow(-1.0,i+1);
        y=1.0/((2*i-1)*(2*(i+1)-1));
        z=x*y;
        sum+=z;
    }
    pi=sum*4.0;
    printf("pi=%.6f \n",pi);
}

```

(3)

```

#include <stdio.h>
#include <math.h>
#include <stdlib.h>
void main()
{
float i,x,y,z,pi,sum=0.0;
    for(i=1.0;i<=1000000.0;i++){
        x=pow(-1.0,i+1);
        y=1.0/(2*i-1);
        z=x*y;
        sum+=z;
    }
    pi=sum*4.0;
    printf("pi=%.6f \n",pi);
}

```

Results :

(1) when  $i \leq 10$  ,pi=3.109625  
when  $i \leq 100$  ,pi=3.138408  
when  $i \leq 1000$  ,pi=3.141273  
when  $i \leq 10000$  ,pi=3.141459  
when  $i \leq 100000$  ,pi=3.1414597 (same as  $i \leq 10000$ )  
The value convergence at 3.14145970344543457000 when  $i \leq 10000$

(2) when  $i \leq 10$  ,pi=3.137078  
when  $i \leq 100$  ,pi=3.141544  
when  $i \leq 1000$  ,pi=3.141593  
when  $i \leq 10000$  ,pi=3.141593 (same as  $i \leq 1000$ )  
The value convergence at 3.14159321784973145000 when  $i \leq 1000$

(3) when  $i \leq 10$  ,pi=3.041839  
when  $i \leq 100$  ,pi=3.131593  
when  $i \leq 1000$  ,pi=3.140593  
when  $i \leq 10000$  ,pi=3.141499  
when  $i \leq 100000$  ,pi=3.141585  
when  $i \leq 1000000$  ,pi=3.1415954  
The value convergence at 3.14159536361694336000 when  $i \leq 1000000$

Conclusion :

三個算式都將收斂於圓周率，但是，收斂的速度不同，目前測試之結果為  
( 2 ) > ( 1 ) > ( 3 )。